MASSACHUSETTS INSTITUTE OF TECHNOLOGY

DEPARTMENT OF PHYSICS

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Practice Exam 3 Solutions

Problem 1: I fareg Fy = may ay = 0 since

+y my my -Fareg = 0 (Vy)term 1s a

constant!

a)
$$d = V_{term}t = 7 t - d = \frac{1.6 \text{ km}}{50 \times 10^{14} \text{ km}} = 32 \text{ s}$$

b) $W_{g} \text{ rav} = mg d = (80 \times 10^{16} \text{ kg})(9.5 \text{ m})(1.6 \times 10^{3} \text{ m}) = 1.25 \times 10^{6} \text{ J}$

c) $W_{d} \text{ ray} = -\frac{mg d}{t} = -\frac{1.25 \times 10^{6}}{3.2 \times 10^{16}} = -3.92 \times 10^{16} \text{ W}$

d) $P_{d} \text{ reg} = \frac{W_{d} \text{ rag}}{t} = -\frac{mg d}{t} = -\frac{1.25 \times 10^{16}}{3.2 \times 10^{16}} = -3.92 \times 10^{16} \text{ W}$

e) $E_{d} \text{ reg} = W_{d} \text{ rag} = -\frac{mg d}{t} = -3.92 \times 10^{16} \text{ W}$. Thus

energy shows up as heat; heating both

the skydiver and the air.

Problem 3:

1 Trug Frok = may heat

2 Trug Frok = may heat

2 Trug Frok = may heat

2 Trug Frok = may heat

3 Trug Frok = may heat

4 Trug Frok = may heat

1 Trug Frok = may heat

1 Trug Frok = may heat

2 Trug Frok = may heat

2 Trug Frok = may heat

2 Trug Frok = may heat

3 Trug Frok = may

a) Med. Energy is conserved since T is always perpendicular to the displacement AK+DP. E. = Wn.c. 1 m(v,2-v2) + mg(al) = 0 30/vm, for 2= 2 - 29 (21) $v_{f} = \left((7.0 \, \text{m/s})^{2} - (2)(9.8 \, \text{m}) \right)^{1/2} = 5.4 \, \frac{\text{m}}{\text{s}}$ b) $T = m v_f^2 - m g = m(v_0^2 - 2g(2l)) - m g$ $T = m v_0^2 - 5 m g = (.1/2)(7.0 m)^2 - (5)(.1 kg)(9.5 m)$ (.5 m)Problem 3:

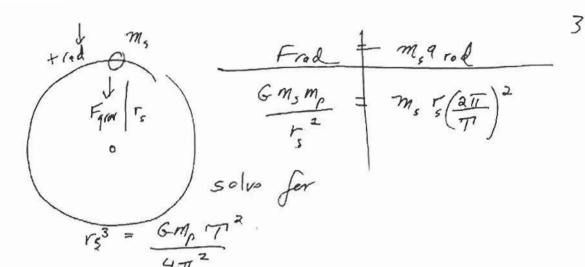
the pen should have zero

velouty at a

to Roty Energy is conserved

xfo xfo xfo y = 0

vo = v = 0 0+ 1k(x2-x2)- 6m, m2(1-1) = 0 $-\frac{1}{2}kX_{0}^{2}+6\frac{m_{1}m_{2}}{R_{p}}=0 \implies X_{0}^{2}=\frac{26m_{1}m_{2}}{R_{p}k}$ $X_0 = \left(\frac{(-3)(6.67 \times (c^{-11} N - m^2)(.01 \log)(2.6 \times (0^{15} \log))}{(5.0 \times 10^3 m)(400 N/L)}\right)^{1/2} = .042 m = 4.2 cm$



$$I_{S} = \left(\left(6.67 \times 10^{-11} \frac{N - m^{2}}{k_{q}^{2}} \right) \left(2.6 \times 10^{-15} \frac{1}{k_{q}^{2}} \right) \left(2.6 \times 10^{-15} \frac{1}{k_{$$

$$r_s = 6.1 \times 10^3 \text{ m}$$

$$v_s = \frac{2\pi r_s}{T} = \frac{(2\pi)(6.1 \times 10^3 \text{ m})}{(7.2 \times 10^3 \text{ sec})} = 5.3 \text{ m/s}$$

d) At the redius is, the conservation of mechanical energy can be used to columbte the velocity of the pen

So eg/1) becomes
$$\frac{1}{2} \frac{m_z v^2 - 6m_z m_z}{r_s} = 0$$

 $v' = \left(\frac{26m_l}{r_s}\right)^{V_z} = \left(\frac{(2)(6.67 \times 10^{-11} N - m^2)(2.6 \times 10^{15} \text{kg})}{k_g^2}\right)^{V_z}$
 $v' = 7.54 \text{ m/s}$

momentum is conserved because there are no external forces. energy is not conserved due to the explosion.

$$\Delta \rho_{\chi} = 0$$

$$m_{\chi} v_{2} - m_{1} v_{1} = m v = 0$$

$$v_{2} = m v + m_{1} v_{1} = (2.0 \text{ Kg})(2.0 \text{ m}) + (0.5 \text{ kg})(1.0 \times 10^{1} \text{ m})$$

$$= 6 \text{ m/s}$$

DKE = Wn.c 1 m2 v2 + 1 m, v2 - 1 m v2 = Wn.c. (1)(1.5kg)(6m)2+(1/2)(.5kg)(10m)2-1(2.0kg)(2.0m)2=48 J 15 the increase on kinetic energy due to 460 explosion. m2 62.f=+450 $\Delta P_{x} = 0 \Rightarrow P_{x,o} = P_{x,f}$ m, v,, - m2 v2, = m2 v2, f cos 62, f DDy = 0 => Py.o= Py.f 0 = m, v,f - m2 2,f sm 6,f BK = 0 =7 K0= Kf $\frac{1}{2}m_{1}v_{10}^{2} + \frac{1}{2}m_{2}v_{2,0}^{2} = \frac{1}{2}m_{1}v_{10}^{2} + \frac{1}{2}m_{2}v_{2,p}^{2}$ (3) Additionally we are told that Vif = Vio eglz) can be rewritten using this fact as m2 22, 5 m 82 if = m1 210 eg (1) m2 v2, f (05 62, f = m, V, 0 - m2 V2, 0

50 dividing those equations yulds

tan 8 = \frac{m_1 v_{10} - m_2 v_{2,0}}{m_1 v_{10} - m_2 v_{2,0}}

Problem 8: m - It I be ark tracy strotch from equilibrium position is already a The equilibrium position smo at equilibrium slightly strateled position $m_{ig} - k y_{eq} = 0 = y_{eq} = \frac{m_{ig}}{k}$ Then when the system is stretched an additional distance you at too $\frac{F_y = m_1 q_y}{m_1 q_1 - k(y + y_1 q_1)} = m_1 \frac{d^2y}{dt^2}$ here y is

an arbitrary
stretch from eq. pos -ky = m, diy we get m, d 2 + Ky = 0 single harmonic motion about yes position $y = A \cos \int_{m}^{k} t + B \sin \int_{m}^{k} t$ $A = y_0$, $B = \frac{v_0}{\sqrt{k_m}} = 0$ released from rest V = dy = - KASIN Et + KBCOS KE t period T: [T = 211 =] TP = 211 [m.

we can find the velouty using $y = y_0 \cos \sqrt{\frac{k}{m_1}} t$, $v_y = -\sqrt{\frac{k}{m_1}} y_0 \sin \sqrt{\frac{k}{m_1}} t$

noting that when $\sqrt{\frac{1}{m}} t = \frac{\pi}{2}$, $\cos(\sqrt{\frac{1}{m}}t) = 0$ so y = 0, mass is back at $\log pos$. Also, $s = (\frac{\pi}{2}) = 1$ so

vg - - √E yo at og. pos. tog= 1/2 /m/K

- c) since a new mass $m_2 = zm_1$ $m + o + d = 3m_1$ and $T = 2\pi \sqrt{3m_1}$
- d) since the collision occured when the mass was completely compressed, the velocity was zero, hence for the collision DK = 0, no energy was lost. Therefore, the new system of mass 3 m, well satisfy a new squilbrium condition in 3 m, q = Kyeq! = 7 yeq! = 3 m, g/k and the osullations are about these position,

So the new equilibrium position lowered by 2m, 9

When the rubber bands were fully compressed by yo , the collision occured. The

To with respect to the snew equilibrium positions

The stretch is

Yot 2M, 9

Huno when the system

1s fully stretched, the mess 3M, is at

9 position The original equilibrium

position