

Your Name \_\_\_\_\_ Section \_\_\_\_\_

## HOMEWORK #13 - 8.01 MIT - Prof. Kowalski

Due 4:00PM Thursday Dec. 4, 2003

### Topics: Harmonic Oscillators and Relative Motion

Any following problems designated with a bold number indicate problems from Young and Freedman 11<sup>th</sup> edition.

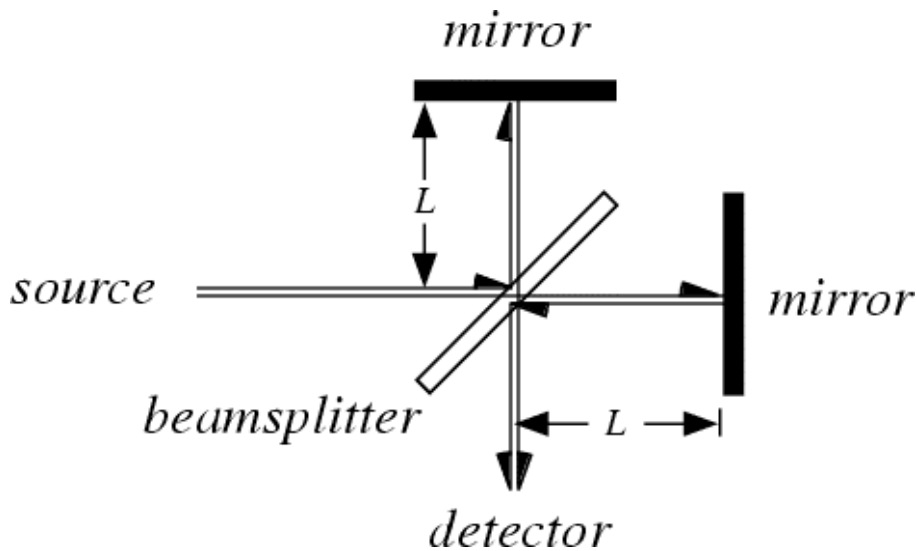
#### 1. Vibration Isolation System

A heavy table of mass  $M$  is vibrationally isolated by being hung from the ceiling by springs so that its period of vertical oscillation is  $\omega_0$  (take  $\omega_0$  to be  $2\pi/\text{sec}$ , a typical value). Assume now that the ceiling vibrates vertically with amplitude  $A$  at frequency  $\omega$ , i.e.  $y_c(t) = A \cos(\omega t)$ .

1. Write down the dynamical equation that relates the acceleration of the table  $a(t)$  to its position  $y(t)$ , and the position of the ceiling. Although  $M$  and  $k$  will appear in this equation, you should be able to replace them with  $\omega_0$ . Show that the equation you get this way is the same as if a force proportional to  $\cos(\omega t)$  were acting on the mass – spring system.

This system is referred to as a **driven harmonic oscillator**. Its steady state solution is  $y(t) = C(\omega) \cos(\omega t)$ . NOTE that it responds solely at the drive frequency  $\omega$ , not at the natural frequency of the oscillator  $\omega_0$ . (Actually there is also a transient at  $\omega_0$  that fades away with time in a real system due to damping.)

2. By substituting the above expression for  $y(t)$  (and the  $a(t)$  that results from this) in your equation from part a, you should be able to obtain and solve a simple equation for  $C(\omega)$ .
  3. With what amplitude,  $y_t$ , will the table oscillate if the building (i.e. ceiling) oscillates with amplitude 0.01 cm at a (typical) frequency of 15 Hz? This ratio is called the isolation factor at  $\omega$ .
- 2. 13.88**
- 3. 37.1** A double lightning bolt strikes opposite ends of a passenger car that is moving with speed  $v$ , lighting up the ends of the car simultaneously from the perspective of a rider in the middle of the car. Which bolt appears to have come earlier to an observer on the ground, or do they appear simultaneous to him?



- 4. Michelson-Morley Experiment with ether.** Michelson, and later Michelson and Morley used a Michelson interferometer mounted on a round granite block that floated on mercury in a surrounding tub. Their experiment is shown above (drawing from <http://hyperphysics.phy-astr.gsu.edu/hbase/relativ/mmhist.html>). Michelson and most physicists of his generation imagined that light propagates through a transparent nearly massless but quite stiff (so the speed of the light relative to the ether is  $c=3 \times 10^8$  m/s) medium called the “ether”. He thought his experiment would detect the motion of the earth through this ether.
- If this experiment is moving to the right at speed  $v$ , find the time difference for the light to traverse back and forth through the distance  $L$  in *both* the horizontal and vertical direction. *Hint: neither time is  $2L/c$*
  - In the Michelson-Morley experiment, the light bounced back and forth several times for a total distance  $L=11\text{m}$ , and the travel time difference was measured as a shift of the interference pattern (where one fringe was  $0.25\ \mu\text{m}$ ). What was the expected fringe shift when the apparatus was rotated through  $90$  degrees assuming that  $v$  is the velocity of the earth in its orbit? (The observed fringe shift was less than  $0.01$  of a fringe.)