

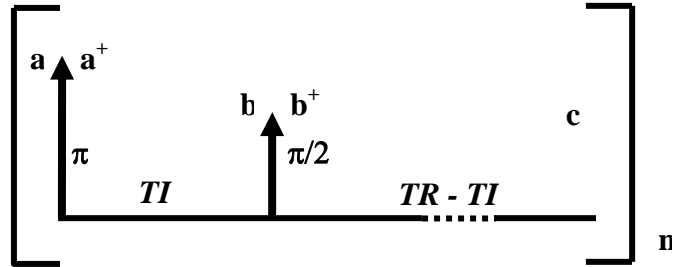
## HST.584 / 22.561 – Problem Set 3

Due: Mar. 22 / 2006 in class

1) Consider the pulse sequence at right:

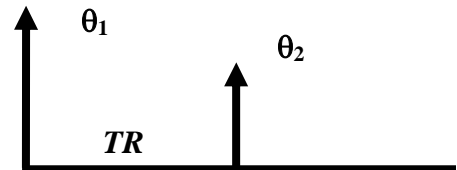
The sequence begins with a  $\pi$  pulse, followed by a delay of  $TI$ , followed by a  $\pi/2$  pulse and another delay  $TR - TI$ , such that the total repetition time for the sequence is  $TR$ .

With respect to the longitudinal magnetization present before the  $\pi$  pulse, and assuming a homogenous  $T_1$  and  $T_2$  for the system under investigation, what are the longitudinal and transverse components of magnetization at points  $\mathbf{a}^+$ ,  $\mathbf{b}$ ,  $\mathbf{b}^+$  and  $\mathbf{c}$ ? At what point after the  $\pi/2$  pulse will the signal be maximized? If the pulse sequence is repeated, what will be the steady state signal amplitude (i.e. transverse magnetization at the start of the FID) be, as a proportion of the equilibrium magnetization of the system  $\mathbf{M}_{tot}$ ?



2) Consider the following pulse sequence in which an RF excitation pulse of tip angle  $\theta_1$  is followed by a  $\theta_2$  pulse a fixed time,  $TR$  later. Assume the following throughout:

- the object is homogenous with a single value of  $T_1$  and  $T_2$
- the magnetization is initially at equilibrium ( $M_0$ )
- $TR$  is much longer than  $T_2$  ( $TR \gg T_2$ )
- $T_1 = 5TR$



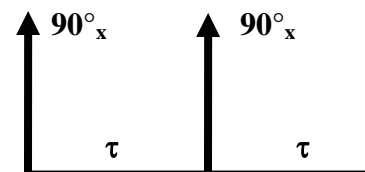
a) If  $\theta_1 = \theta_2 = 60^\circ$ , what are the relative signal amplitudes (immediately after the excitation) for the two FIDs?

b) Determine  $\theta_1$  such that the FID amplitude from the second excitation is always zero.

c) Determine  $\theta_2$  if  $\theta_1 = 25^\circ$ , to produce equal signal amplitudes for the two FIDs.

d) Determine the  $\theta_1$  and  $\theta_2$  combination that produces the maximum possible signal amplitudes (they must still be equal and ignore  $T_1$  effects).

3) Compare a conventional  $90^\circ_x - \tau - 180^\circ_x$  spin-echo generating sequence with a  $90^\circ_x - \tau - 90^\circ_x$  sequence as shown below. Ignore  $T_1$  and  $T_2$  relaxation.



a) Given an off-resonance spin that precesses (in the rotating frame) by angle  $\phi$  during the interval  $\tau$ , what is its resultant magnetization at time  $2\tau$ ?

b) If a uniform object contains an ensemble of off-resonance spins such that the precession angle  $\phi$  (after an interval of  $\tau$ ) is uniformly distributed from 0 to  $2\pi$  radians, determine the relative sizes of the net transverse magnetizations at time  $2\tau$  produced by the two sequences. The net transverse magnetization is based on the integration of the transverse component over the entire ensemble.

c) Repeat part (b) by comparing the net transverse magnetization at time  $2\tau$  of a  $90^\circ_x - \tau - 180^\circ_x$  sequence with that of a  $\theta_x - \tau - \theta_x$  sequence.

**Note: Using rotation matrices in this question may be useful.**