

$$\phi = V_{\infty} x + \frac{\Lambda}{4\pi} \ln((x-d)^2 + y^2)$$

$$a) \quad u = \frac{\partial \phi}{\partial x} = V_{\infty} + \frac{\Lambda}{2\pi} \frac{x-d}{(x-d)^2 + y^2}$$

$$v = \frac{\partial \phi}{\partial y} = \frac{\Lambda}{2\pi} \frac{y}{(x-d)^2 + y^2}$$

at $x, y = 0, 0$, require $u = 0$

$$\text{or } V_{\infty} - \frac{\Lambda}{2\pi d} = 0$$

$$2\pi V_{\infty} d = \Lambda \quad (1)$$

at $x, y = d, \sqrt{Cd}$, require $\frac{v}{u} = \frac{dy}{dx}$, where $\frac{dy}{dx} = \frac{1}{2} \sqrt{\frac{C}{x}} \Big|_{x=d} = \frac{1}{2} \sqrt{\frac{C}{d}}$

$$\text{or } \frac{1}{V_{\infty}} \frac{\Lambda}{2\pi} \frac{\sqrt{Cd}}{Cd} = \frac{1}{2} \sqrt{\frac{C}{d}}$$

$$\Lambda = \pi V_{\infty} C \quad (2)$$

$$\text{Combine (1) \& (2)} \rightarrow C = 2d \rightarrow \boxed{d = C/2}$$

b) For $C = 500 \text{ m}$, $V_{\infty} = 15 \text{ m/s}$, $\rightarrow d = 250 \text{ m}$, $\Lambda = 7500\pi \text{ m}^2/\text{s}$

Maximum radius where $v = 1 \text{ m/s}$

$$\text{or } v = \frac{\Lambda}{2\pi} \frac{y}{r^2} = \frac{\Lambda}{2\pi} \frac{\sin \theta}{r} = 1 \text{ m/s}$$

$$\rightarrow \boxed{r_{\max}(\theta) = \frac{\Lambda}{2\pi \cdot 1 \text{ m/s}} \sin \theta = 3750 \text{ m} \cdot \sin \theta}$$

circle of diameter 3750 m above source.

